

Bed Non-uniformity Effects on the Flow Resistance Equations in High-gradient Streams

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ABSTRACT

Reach averaged flow velocity estimates in high-gradient streams vary as sediment becomes poorly sorted, probably due to sediment clustering or armoring. Here we present a semi-empirical approach using the **geometric standard deviation of bed material to calculate the flow velocity**. The high-gradient streams usually contain large clasts, but when particles of size range D_{50} - D_{84} are in a large proportion (poorly sorted), the conventional flow resistance equations must be used with caution to estimate the flow velocity, which is an important hydrometric variable.

OBJECTIVES

Sediment Sorting

1 To evaluate performances of conventional flow resistance equations for sediment non-uniformity (σ_g)

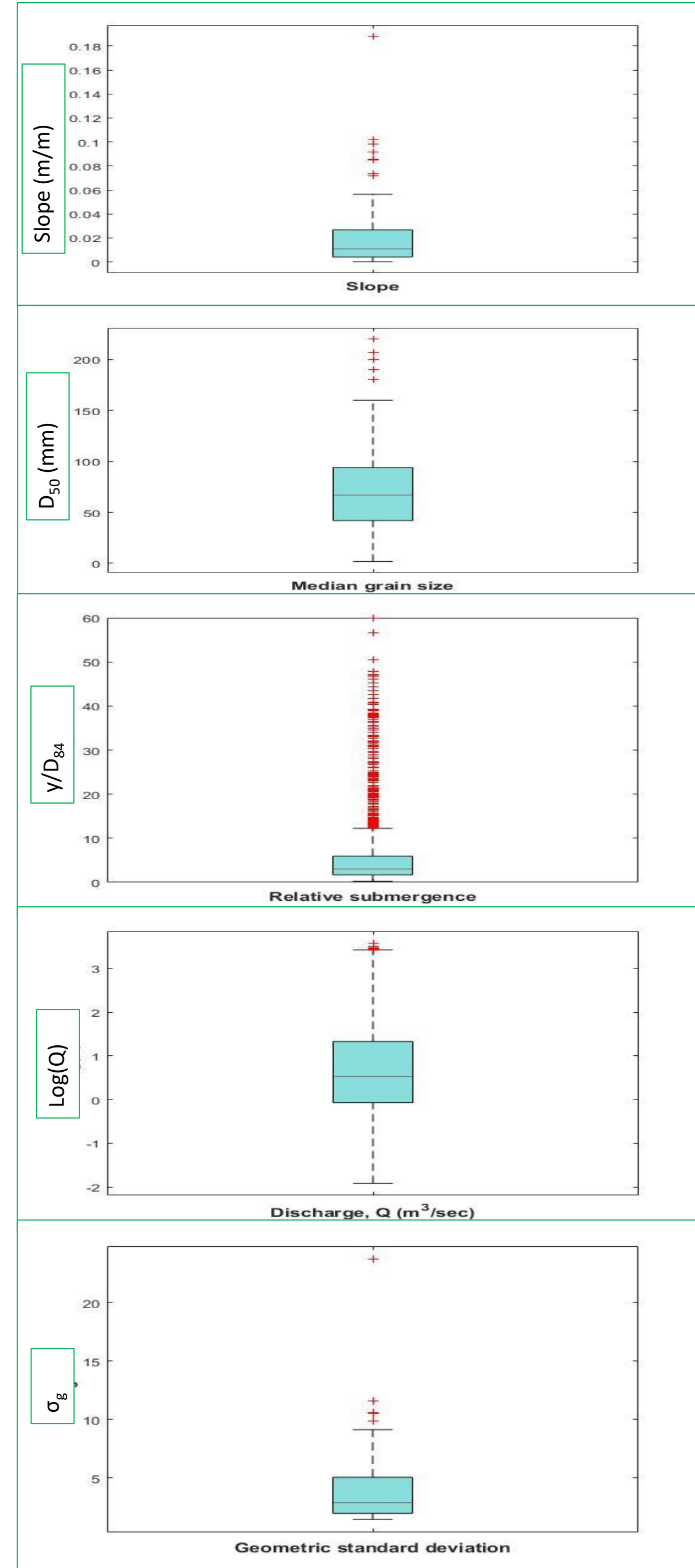
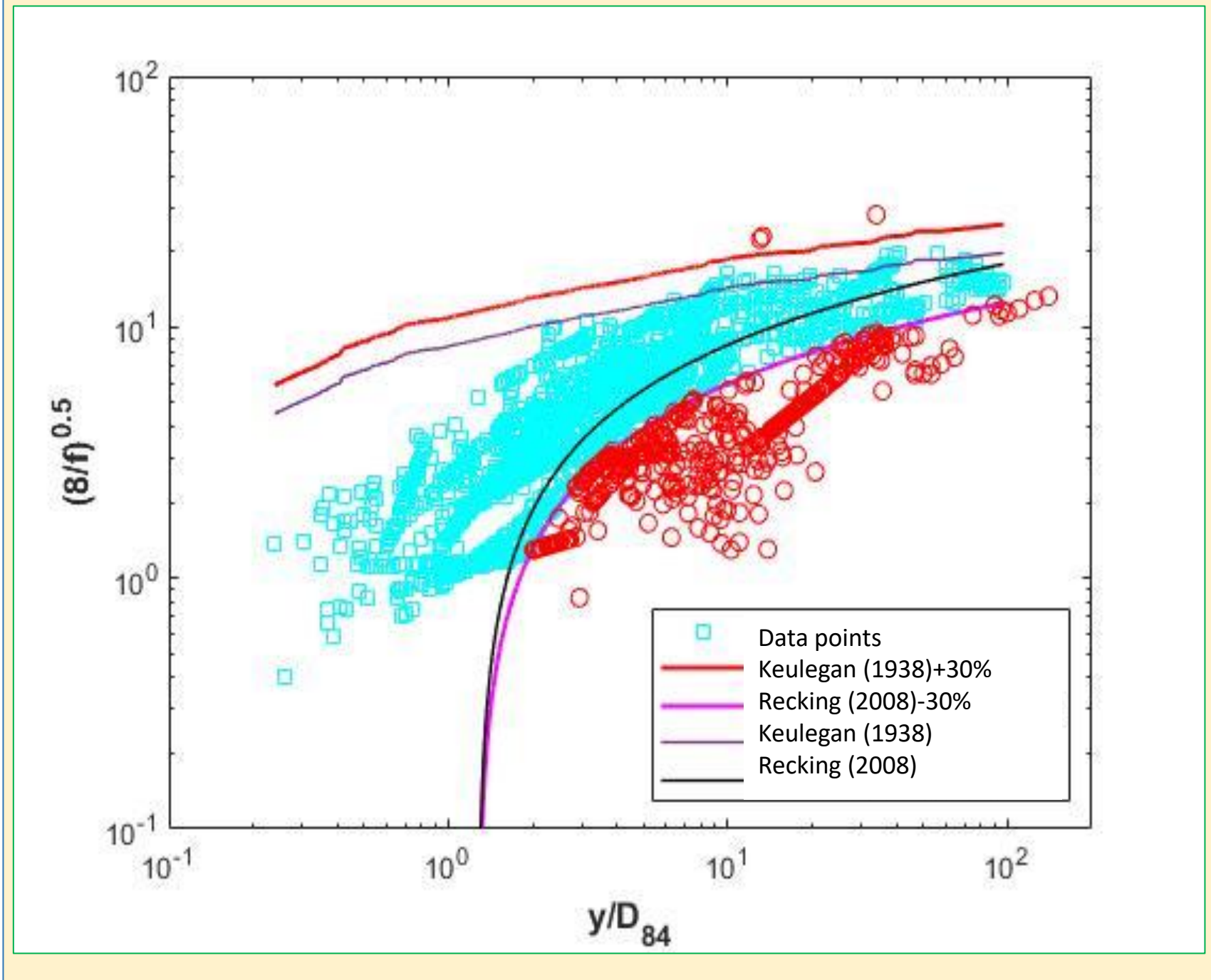
Active Sediment Transport

2 To test the effects of sediment transport on flow resistance

New Semi-empirical Approach

3 To improve the performances of conventional equations using geometric standard deviation, σ_g as an additional term

- 2184 measurements (Mendicino and Colosimo, 2019; Misset et al., 2019)
- Data shortlisted as per criteria suggested by Rickenmann and Recking (2011)
- Calibration dataset -1530 measurements (~70%)
- Validation dataset- 654 measurements (~30%)



DATASET

FLOW RESISTANCE EQUATIONS

Strickler (1923) $\sqrt{\frac{8}{f}} = \frac{u}{u_*} = 8.3 \left(\frac{y}{D_{90}}\right)^{1/6}$

Keulegan (1938) $\sqrt{\frac{8}{f}} = \frac{u}{u_*} = 6.25 + 5.75 \log \frac{y}{D_{50}}$

Hey (1979) $\sqrt{\frac{8}{f}} = \frac{u}{u_*} = 6.25 + 5.75 \log \left(\frac{y}{3.5D_{84}}\right)$

Smart and Jäggi (1983) $\sqrt{\frac{8}{f}} = \frac{u}{u_*} = 5.75 \left[1 - \exp\left(-0.05 \frac{y}{D_{90}} \cdot \frac{1}{\sqrt{S}}\right)\right]^{0.5} \log\left(8.2 \frac{y}{D_{90}}\right)$

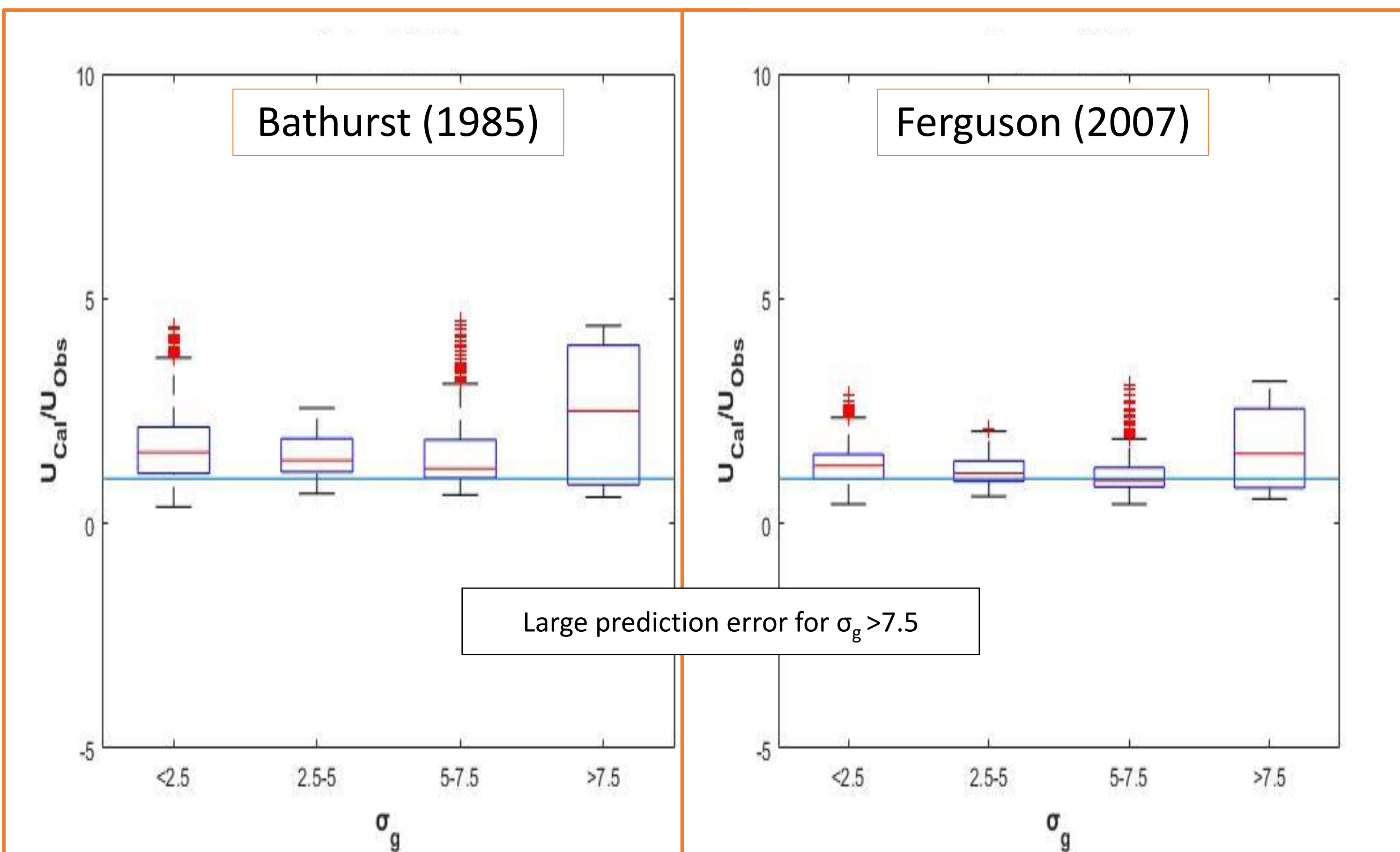
Bathurst (1985) $\sqrt{\frac{8}{f}} = \frac{u}{u_*} = 4 + 5.62 \log \frac{y}{D_{84}}$

Ferguson (2007) $\sqrt{\frac{8}{f}} = \frac{u}{u_*} = \frac{a_1 a_2 \left(\frac{y}{D_{84}}\right)}{\sqrt{a_1^2 + a_2^2 \left(\frac{y}{D_{84}}\right)^{5/3}}}$

Recking et al. (2008) $\sqrt{\frac{8}{f}} = \frac{u}{u_*} = -1 + 9.5 \log \frac{y}{D_{84}}$

Rickenmann and Recking (2011) $\sqrt{\frac{8}{f}} = \frac{u}{u_*} = \frac{4.416 \left(\frac{y}{D_{84}}\right)^{1.904}}{\left[1 + \left(\frac{y}{1.283 D_{84}}\right)^{1.618}\right]^{1.083}}$

SEDIMENT SORTING EFFECTS



Similar results were found for other equations also

BEDLOAD EFFECTS

The measurements characterized by bed load were identified by Shield's stress, Y , with its critical value, $Y_{CR}=0.029$ (Ackers and White, 1973)

$$Y = \frac{u_*^2}{g D_{84} (G-1)}$$

Equations	Statistical indices	Conventional equations using the whole dataset	
		($Y/Y_c < 1$) N=1597	($Y/Y_c \geq 1$) N=587
Smart and Jaggi (1983)	RMSE	0.37	0.51
	RMSPE	4.79	7.70
Bathurst (1985)	RMSE	0.45	0.94
	RMSPE	7.39	18.43

NEW MODIFIED EQUATIONS

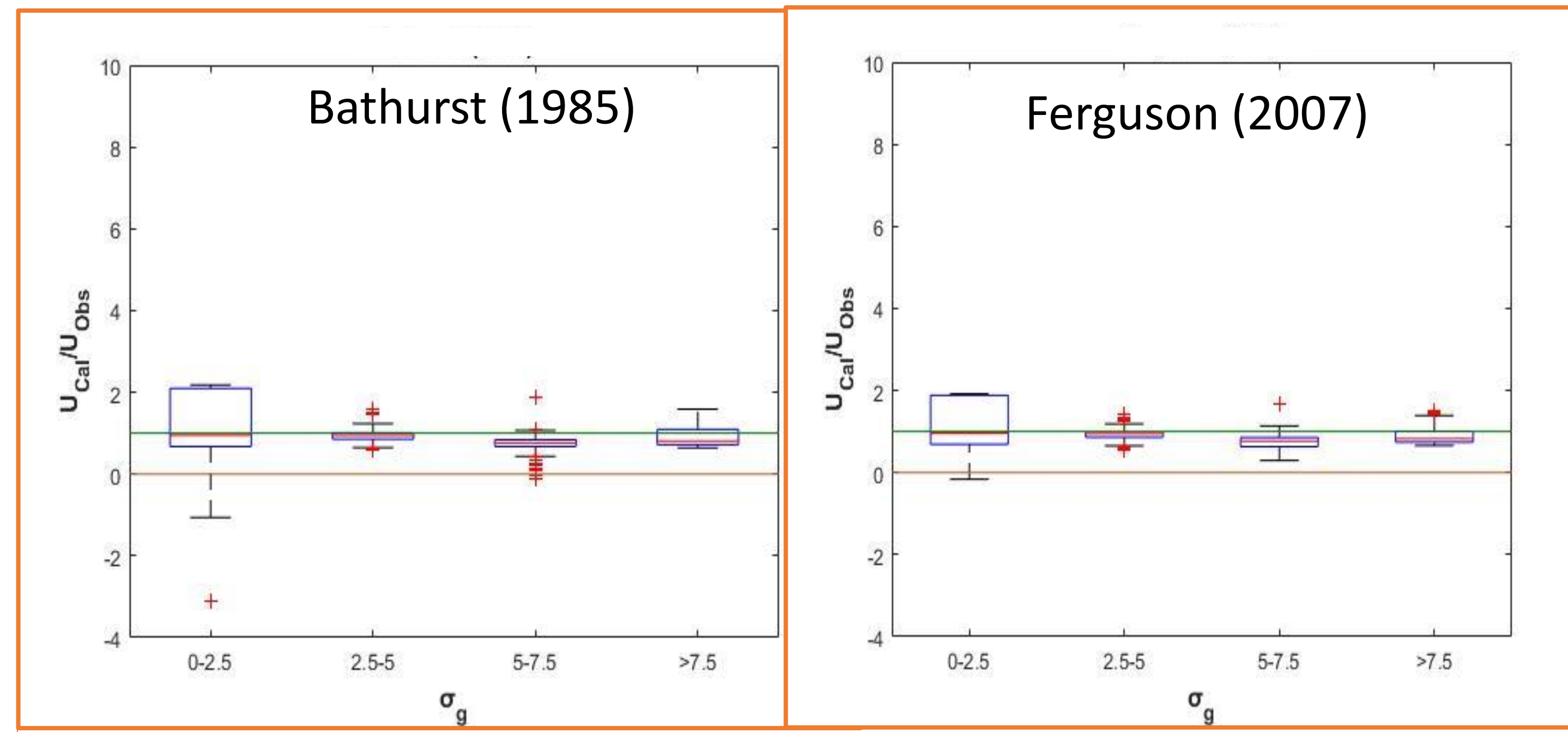
Modified equation = Conventional equation + $f(\sigma_g)$
 $f(\sigma_g) = a_1(\sigma_g)^{a_2} + a_3$

Modified Ferguson (2007) equation would be expressed as:

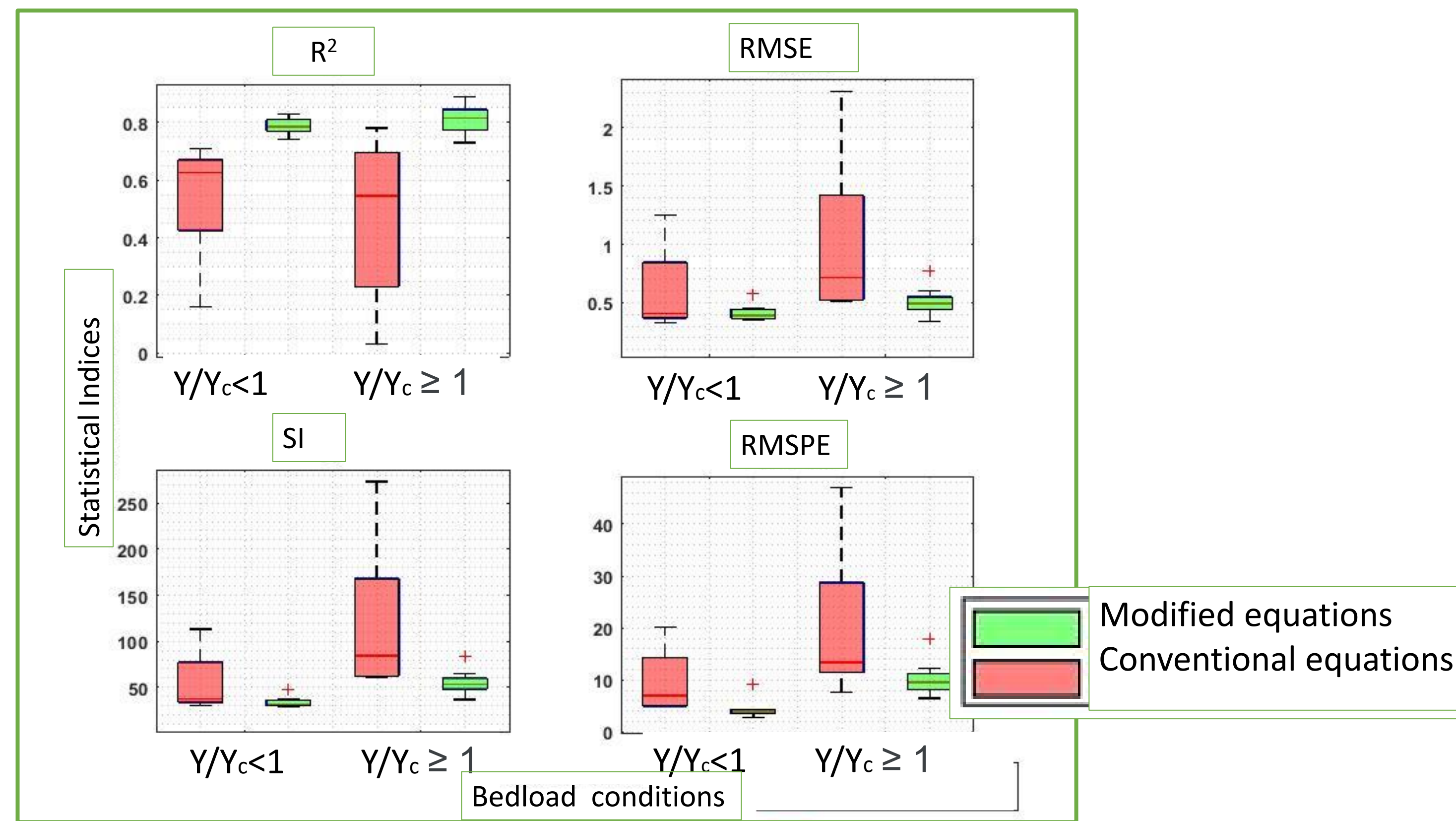
$$\sqrt{\frac{8}{f}} = \frac{u}{u_*} = \frac{a_1 a_2 \left(\frac{y}{D_{84}}\right)}{\sqrt{a_1^2 + a_2^2 \left(\frac{y}{D_{84}}\right)^{5/3}}} + a_1(\sigma_g)^{a_2} + a_3$$

Minimizing the difference between observed and calculated values $\rightarrow a_1=8.94, a_2=0.04, a_3=-10$

VALIDATION



Similar results were found for other equations also



Equation	Conventional Equations		Modified Equations		Δ AIC	Δ BIC
	AIC	BIC	AIC	BIC		
Ferguson (2007)	1179.9	1202.3	1156.1	1191.9	23.8	10.4

CONCLUSIONS

Similar results were found for other equations also

- The conventional equations are **reliable in case of large submergence, uniform bed material and no sediment transport conditions**.
- The modified equations are **capable to consider the additional losses** occurring in case of poorly sorted sediments during bedload transport
- The inclusion of bed statistics, particle arrangement and microtopography of the bed might improve the predictive capability of conventional flow resistance equations.

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